Outline and preliminaries
Modelling distribution and growth: a generic model
Modelling distribution and growth: PK variants
Extensions/new developments
Summary and conclusions
References

Distribution and Growth

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Modelling distribution and growth: a generic model Modelling distribution and growth: PK variants Extensions/new developments Summary and conclusions References

Plan of lecture

- Preliminaries: some basic terms and concepts
- A generic model
- Post-Keynesian variants (Kalecki-Robinson tradition)
 - the neo-Keynesian model
 - the Kalecki-Steindl model
 - the Bhaduri-Marglin model
- Extensions and new developments
 - autonomous-demand-led exogenous growth
 - shifting equilibrium, pseudo instability, and cyclical growth
 - monetary and financial determinants of growth
 - debt-financed consumption spending and the accumulation of household debt
 - wage inequality
 - technical change and the supply side
- Summary and conclusions



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Some preliminaries

- ▶ Distribution of *what*? opportunity, wealth, **income**
- Among whom? gender, race, class
- How measured size distribution (Gini, Theil indices; Palma ratio etc.), functional distribution (wages vs. profits)

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Some preliminaries (cont.)

Why study distribution and growth?

Predominant answer: role of distribution in growth process

- ► Endogenous (adjusting) variable) variable, that facilitates movement into steady-state equilibrium
 - neo-Keynesian models (Robinson, Kaldor, Pasinetti)
- Exogenous variable determinant of steady-state equilibrium configuration
 - profit-led (classical PE)
 - wage-led (Kaleckian Dutt, Lavoie)
 - wage- or profit-led (Bhaduri-Marglin)



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Some preliminaries (cont.)

BUT:

- Distribution important in its own right
- Focus on growth process ≠ advocacy of hyper-expansion
 - e.g., de-growth or zero growth how achieved? Implications for distribution?

ALSO - doesn't growth affect distribution?

 Yes, but at higher frequency (short cycles vs secular (long-term) growth)



Model foundations

- Assume two-class economy (workers, capitalists)
- Assume Leontieff production technology
- Assume closed economy with no fiscally-active government sector, all consumption funded by current income
 - investment the only (potential) source of autonomous demand
- ► Then ...

Basic accounting identity:

$$wN + \Pi \equiv Y \equiv C_W + C_\Pi + I$$

From $Y \equiv wN + \Pi$:

$$1 \equiv \frac{wN}{Y} + \pi$$

$$\Rightarrow \pi = 1 - wa \tag{1}$$

where $\pi \equiv \Pi/Y$ and $a \equiv N/Y$



Also from $Y \equiv wN + \Pi$:

$$\frac{Y}{K} \equiv \frac{wN}{K} + r$$

$$\Rightarrow r \equiv \frac{Y}{K} - \frac{wY}{K} \cdot \frac{N}{Y}$$

$$\Rightarrow r = \frac{Y}{K} (1 - wa)$$

$$\Rightarrow r = \frac{Y}{K_u} \cdot \frac{K_u}{K} (1 - wa)$$

$$\Rightarrow r = \frac{\pi u}{v}$$
(2)

where $u \equiv K_u/K$ and $v \equiv K_u/Y = K/Y_p$

Note that:

a) If
$$u = \bar{u}_n = 1$$
:

$$r = \frac{\pi}{v} = \frac{1}{v}(1 - wa)$$

$$\Rightarrow \frac{dr}{dw} = -\frac{a}{v} < 0$$

Result: classical wage-profit frontier – strict trade-off between *w* and *r*



b) If
$$u \neq \bar{u}_n = 1$$
:
$$r = \frac{\pi u}{v} = \frac{u}{v}(1 - wa)$$

$$\Rightarrow \frac{dr}{dw} = \frac{\partial r}{\partial \pi} \cdot \frac{d\pi}{dw} + \frac{\partial r}{\partial u} \cdot \frac{du}{dw}$$

$$\Rightarrow \frac{dr}{dw} = -u\frac{a}{v} + \frac{1}{v}(1 - wa) \cdot \frac{du}{dw}$$

Result: No strict trade-off between w and r

Outline and preliminaries

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Model foundations (cont.)

Two important lessons emerge, even at this early stage:

- ► Importance of *closures*
- Importance of treatment of u

From
$$wN + \Pi \equiv C_W + C_\Pi + I$$
:
$$wN + \Pi = c_W wN + c_\Pi \Pi + I$$

$$\Rightarrow (wN - c_W wN) + (\Pi - c_\Pi \Pi) \equiv S = I$$

where c_w and c_Π are marginal propensities to consume from wages and profits, respectively.

Now assume $c_W=1$ (Kalecki – workers "spend what they get") and define $s_\Pi\equiv 1-c_\Pi$. It follows that:

$$s_{\Pi} \Pi = I$$

$$\Rightarrow s_{\Pi} \frac{\Pi}{K} = \frac{I}{K}$$

$$\Rightarrow r = \frac{1}{s_{\Pi}} g$$

$$\Rightarrow g^{s} = s_{\Pi} r \tag{3}$$

where $g \equiv I/K$ and $g^s = g|_{I=S}$



Note: g is both 'rate of accumulation' and (long-term) 'rate of growth', since:

$$v \equiv \frac{K_u}{Y}$$

$$\Rightarrow \hat{Y} - \hat{K}_u|_{u = \bar{u}} = 0$$

$$\Rightarrow \hat{Y} = \hat{K}_u|_{u = \bar{u}}$$

$$\Rightarrow \hat{Y} = g$$

To recap, we have so far established that:

$$\pi = 1 - wa \tag{1}$$

$$r = \frac{\pi u}{v} \tag{2}$$

$$g^s = s_{\Pi} r \tag{3}$$

We've now reached a 'fork in the road'.

Consider two additional (alternative) closures:

- ▶ $I \equiv S \Rightarrow g \equiv g^s$ classical Marxian model
- ▶ $I \not\equiv S$, g = g(.) Post-Keynesian model

Complete (generic) PK model can therefore be summarized as:

$$\pi = 1 - wa \tag{1}$$

$$r = \frac{\pi u}{v} \tag{2}$$

$$g^s = s_{\Pi} r \tag{3}$$

$$g = g(.) \tag{4}$$



Key in what follows will be:

- ▶ Different assumptions about u ($u = \bar{u}_n = 1$ vs. $u \neq \bar{u}_n = 1$)
- ▶ Different assumptions about g(.)

Joan Robinson's neo-Keynesian model

- Robinson (1956, 1962) can be considered the 'root' of contemporary PK theory of distribution and growth
- Robinson model is neo-Keynesian not Kaleckian (despite origins in Kalecki's two-sided relationship between investment and profits)
- ▶ A look at the structure and adjustment mechanisms of Robinson's model reveals nature of neo-Keynesian approach and (as will become clear) sets us up for investigation of subsequent Kaleckian developments

Assume $u = \bar{u}_n = 1$. Then:

$$r = \frac{\pi u}{v} = \frac{1}{v}(1 - wa) \tag{2}$$

This is the classical wage-profit frontier

Investment function:

$$g = g(r^e)$$

or:

$$g = \gamma_1 + \gamma_2 r^e \tag{5}$$

Complete model:

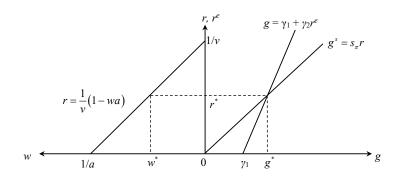
$$r = \frac{1}{v}(1 - wa) \tag{2}$$

$$g^s = s_\pi r \tag{3}$$

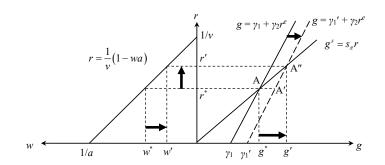
$$g = \gamma_1 + \gamma_2 r^e \tag{5}$$

To solve, set $r=r^e$ and assume Keynesian stability condition $s_{\pi}>\gamma_2$:

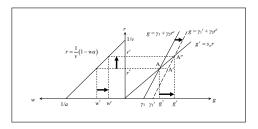




- Now suppose an improvement in animal spirits raises γ_1
- ► This will:
 - increase the rate of accumulation, which will ...
 - increase the equilibrium rates of growth and profit, and ...
 - ... decrease the equilibrium real wage

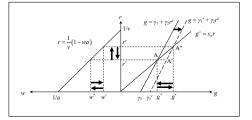


- What's happening is:
- ► *I* > *S* bids up prices in the goods market ...
- ... which lowers w ...
- ... which raises r ...
- ... which raises g



An aside: the inflation barrier

- Assume that w* is a minimum wage
- ► Then as $I > S \Rightarrow \uparrow P$ in the goods market ...
- ► ... $w < w^* \Rightarrow \uparrow W$ in the labour market
- ▶ So $\uparrow P \Rightarrow \uparrow W \Rightarrow \uparrow P$ etc.
- Nominal dynamic wage-price inflationary spiral



Neo-Keynesians versus Kaleckians

- ▶ How "truly" Keynesian is the Robinson model?
 - it's demand-led
 - ▶ BUT excess demand in the goods market resolved by price adjustment – and hence real wage adjustment, and hence change in the distribution of income
 - distribution is the adjusting variable that enables the model to 'get into' equilibrium ...
 - ightharpoonup ... and necessarily so, because $u=\bar{u}_n=1$ prevents alternative quantity adjustment channel
- These observations/criticisms are the fundamental point of departure for Kaleckians



Neo-Keynesians versus Kaleckians (cont.)

- ▶ If the complaint with the Robinson model is that it relies on price adjustment in the goods market ...
- ightharpoonup ... and if this is inevitable because $u=\bar{u}_n=1$ prevents quantity adjustment ...
- ... then the solution is simple: relax the assumption that $u = \bar{u}_n = 1$

Neo-Keynesians versus Kaleckians (cont.)

- This is the basis of Kaleckian theory, which treats u as variable
- Note: transition from neo-Keynesian to Kaleckian theory is analytically simple (relax $u = \bar{u}_n = 1$)
- ▶ But the consequences are profound:
 - investment function modified
 - (important) relationship between distribution and growth transformed
- ► And the behavioural basis for treating *u* as variable remains controversial



The Kaleckian model

In the Kaleckian model:

$$r = \frac{\pi u}{v} \tag{2}$$

is called the *pricing equation*.

This is because in the Kaleckian theory of the firm:

$$\Rightarrow 1=(1+ au)wa$$
 $\Rightarrow \pi=1-wa=rac{ au}{1+ au} \quad ext{and} \quad w=rac{1-\pi}{a}=rac{1}{(1+ au)a}$

 $P = (1 + \tau) Wa$

In other words, both π and w are now fixed, determined by the mark up (τ) chosen by firms in the pricing decision.

Recall also that with u now treated as variable:

$$r = \frac{\pi u}{v} = \frac{u}{v}(1 - wa) \tag{2}$$

This is just the reformulated classical wage-profit frontier derived earlier

But with $w = \frac{1-\pi}{a} = \frac{1}{(1+\tau)a}$, variation in u is now the only source of variation in r

Investment function:

$$g = g(u^e, r^e)$$

or:

$$g = \gamma + g_u u^e + g_r r^e$$

Note that since:

$$r = \frac{\pi u}{v} \tag{2}$$

it follows that:

$$u = \frac{vr}{\pi}$$

$$\Rightarrow u^e = \frac{vr^e}{\pi}$$

if firms form expectations consistently (but see Lavoie (2003); Dallery and van Treeck (2011))



Hence upon substitution, the investment function can be re-written as:

$$g = \gamma + \frac{g_u v}{\pi} r^e + g_r r^e$$

$$\Rightarrow g = \gamma + \left(g_r + \frac{g_u v}{\pi}\right) r^e \tag{6}$$

Complete model:

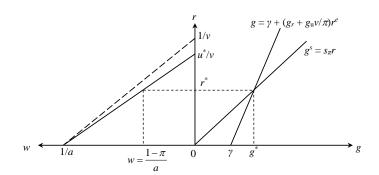
$$r = \frac{\pi u}{v} = \frac{u}{v}(1 - wa) \tag{2}$$

$$g^s = s_\pi r \tag{3}$$

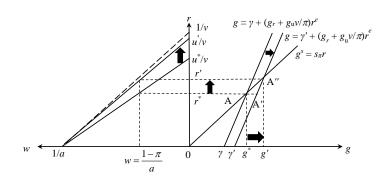
$$g = \gamma + \left(g_r + \frac{g_u v}{\pi}\right) r^e \tag{6}$$

To solve, once again set $r=r^e$ and assume Keynesian stability condition $s_{\pi}>g_r+\frac{g_uv}{\pi}$:

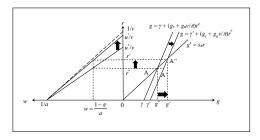




- lacktriangle Now suppose an improvement in animal spirits raises γ
- This will:
 - increase the rate of accumulation, which will ...
 - increase the equilibrium rates of growth and profit, and ...
 - ... increase the equilibrium capacity utilization rate, with the real wage (distribution of income) unchanged



- ► What's happening is:
- I > S increases sales and production in the goods market ...
- ... which raises u ...
- ... which raises r ...
- ... which raises g



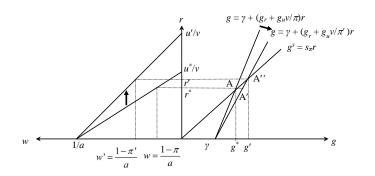
Neo-Keynesians versus Kaleckians again

- Note, then, that having relaxed the assumption that $u = \bar{u}_n = 1$, we've gone from:
 - price adjustment in the Robinson model to
 - quantity adjustment in the Kaleckian model
- Or, in other words, from:
 - exogenous capacity utilization and endogenous distribution (Robinson model) to
 - exogenous distribution and endogenous capacity utilization (Kaleckian model)
- ► These orthogonal dimensions of adjustment need not be treated as mutually exclusive, of course (Lavoie, 2010)



The paradox of costs

- Suppose now that we increase the real wage (i.e., decrease the profit share $\pi = 1 wa$)
- ► This involves increasing the costs of production
- BUT in the Kaleckian model, r will rise (as, too, will g and u)
- ► This is the (in)famous paradox of costs
- So how does it work?



No trickery is involved here. Hence note that:

$$g^* = \frac{s_{\pi}\pi\gamma}{(s_{\pi} - g_r) - g_u v}$$

$$\Rightarrow \frac{dg^*}{d\pi} = \frac{-s_{\pi}\gamma g_u v}{[(s_{\pi} - g_r) - g_u v]^2} < 0$$

$$r^* = \frac{\pi\gamma}{(s_{\pi} - g_r) - g_u v}$$

$$\Rightarrow \frac{dr^*}{d\pi} = \frac{-\gamma g_u v}{[(s_{\pi} - g_r) - g_u v]^2} < 0$$

$$u^* = \frac{v\gamma}{(s_{\pi} - g_r) - g_u v}$$

$$\Rightarrow \frac{du^*}{d\pi} = \frac{-(s_{\pi} - g_r)\gamma v}{[(s_{\pi} - g_r) - g_u v]^2} < 0$$

Since if $s_{\pi} > g_r + \frac{g_u v}{\pi}$ (the Keynesian stability condition) and $\frac{g_u v}{\pi} > 0$, it must be that:

$$s_{\pi} > g_r + \frac{g_u v}{\pi} > g_r \Rightarrow s_{\pi} - g_r > 0$$



Notice that by contrast in the Robinson model:

$$g^* = rac{s_\pi \gamma_1}{s_\pi - \gamma_2}$$
 $r^* = rac{\gamma_1}{s_\pi - \gamma_2}$
 $\Rightarrow rac{dg^*}{d\pi} = rac{dr^*}{d\pi} = 0$

No influence of distribution on (equilibrium) growth and profit rates.

- ► Key result of Kaleckian model: economy unequivocally wage-led. Redistribution towards wages:
 - enriches workers (higher w)
 - enriches capitalists at the same time (higher r)
 - ightharpoonup and improves macro performance in the process (higher u, g)
- Win-win-win capitalism!
- And of obvious (massive) contemporary significance
- Or is it too good to be true?

- ► First, note that paradox of costs is a macro result that might be true in principle but difficult (impossible?) to achieve in practice
 - it starts with an increase in w
 - do individual firms have the macro insights to accept this?
 - or will they resist it as a seeming attack on their profitability?

- Second, paradox of costs may be wrong in principle
 - it emerges from a "re-tooling" of the Robinsonian investment function
 - but does this re-tooling "get the investment function right"?
- ► This brings us to third generation PK theory, associated with Bhaduri and Marglin (1990); Marglin and Bhaduri (1990)

Bhaduri-Marglin versus the Kaleckians

Bhaduri-Marglin - if $u \neq \bar{u}_n = 1$ so that:

$$r = \frac{\pi u}{v}$$

and:

$$g = g(r) \tag{7}$$

as in Robinson, then we can write:

$$g = g(\pi, u)$$

The influence of (now assumed variable) u on g is already captured by an essentially Robinsonian investment function!



Bhaduri-Marglin versus the Kaleckians

According to Bhaduri-Marglin, the Kaleckian investment function:

$$g = g(r, u)$$

overcounts the influence of u on g, which enters twice (directly and then again, indirectly, via r)

Bhaduri-Marglin versus the Kaleckians

BUT – this "accounting" argument is controversial. In the Kaleckian tradition:

- ➤ A strong accelerator effect (i.e., large effect of u on g) is to be expected:
 - firms operating objective is to keep pace with the expansion of the goods market, so as to maintain their market share and hence degree of monopoly power
- An *independent* accelerator effect (i.e., separate from *r*) is appropriate:
 - the influence of u and r on g are qualitatively different: u causes g (accelerator effect) whereas r facilitates g (source of finance) (Mott and Slattery, 1994)

But suppose we go along with Bhaduri-Marglin and see where this leads

The Bhaduri-Marglin model

As we've already seen, point of departure for Bhaduri-Marglin involves replacing the Kaleckian investment function:

$$g = g(r, u)$$

with:

$$g = g(\pi, u) \tag{8}$$

NOTE: implicit form of Bhaduri-Marglin function is deliberate: not all functional forms create full suite of Bhaduri-Marglin results



The Bhaduri-Marglin model (cont.)

Complete model:

$$r = \frac{\pi u}{v} = \frac{u}{v}(1 - wa) \tag{2}$$

$$g^s = s_\pi r \tag{3}$$

$$g = g(\pi, u) \tag{8}$$

To solve, set $g = g^s = g^*$:



The Bhaduri-Marglin model (cont.)

$$\frac{s_{\pi}\pi u^*}{v}=g(\pi,u^*)$$

where u^* denotes the equilibrium rate of capacity utilization.

Can't solve explicitly for u^* , but by totally differentiating our equilibrium solution, we get:

$$\frac{du^*}{d\pi} = \frac{g_{\pi} - \frac{s_{\pi}u^*}{v}}{\frac{s_{\pi}\pi}{v} - g_{u}}$$

The paradox of costs again

If the Keynesian stability condition holds, so that:

$$\frac{s_{\pi}\pi}{v}-g_{u}>0$$

Then:

$$\frac{du^*}{d\pi^*} > 0$$
 if $g_{\pi} > \frac{s_{\pi}u^*}{v}$

or:

$$\frac{du^*}{d\pi^*} < 0$$
 if $g_{\pi} < \frac{s_{\pi}u^*}{v}$

- Effect of redistribution on model outcomes now ambiguous
- What's going on what happened to the paradox of costs?!
- ► Clue: everything turns on the responsiveness of the investment function to the profit share (g_{π})
- So let's consider explicit (linear) form of Bhaduri-Marglin investment function
- ► (WARNING: 'traditional' linear g(.) (with positive coefficients) does **not** deliver full suite of Bhaduri-Marglin results (Blecker, 2002) so following exercise is good for intuition only!)

Write:

$$g = g(\pi, u) = \gamma + g_{\pi}\pi + g_{u}u$$

Since:

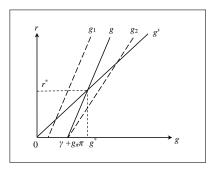
$$r = \frac{\pi u}{v} \Rightarrow u = \frac{vr}{\pi}$$

it follows that:

$$g = g(\pi, u) = \gamma + g_{\pi}\pi + \frac{g_{u}v}{\pi}r$$

Can now see that g varies directly with π via "intercept" term, and indirectly with π via "slope" term.

- ▶ In event of $\pi' < \pi$:
- g₁ captures "intercept effect" (ceteris paribus)
- g₂ captures "slope effect" (ceteris paribus)
- ► Final result ambiguous



The ambiguity so-noted creates *three* different cases in the Bhaduri-Marglin model

To see this, first note that since:

$$r^* = \frac{\pi u^*}{v}$$

it follows that:

$$\frac{dr^*}{d\pi} = \frac{\partial r^*}{\partial \pi} + \frac{\partial r^*}{\partial u^*} \frac{du^*}{d\pi} = \frac{u}{v} + \frac{\pi}{v} \frac{du^*}{d\pi}$$
$$\Rightarrow \frac{dr^*}{d\pi} = \frac{u}{v} \left(1 + \frac{\pi}{u^*} \frac{du^*}{d\pi} \right)$$

Meanwhile, the equilibrium condition $g = g^s = g^*$ means that:

$$g^* = \frac{s_\pi \pi u^*}{v}$$

so that:

$$\frac{dg^*}{d\pi} = \frac{\partial g^*}{\partial \pi} + \frac{\partial g^*}{\partial u^*} \frac{du^*}{d\pi} = \frac{s_\pi u^*}{v} + \frac{s_\pi \pi}{v} \frac{du^*}{d\pi}$$
$$\Rightarrow \frac{dg^*}{d\pi} = \frac{s_\pi u}{v} \left(1 + \frac{\pi}{u^*} \frac{du^*}{d\pi} \right)$$

So in fact, everything turns on the sign and size of:

$$\frac{\pi}{u^*} \frac{du^*}{d\pi}$$

which is the *elasticity of u** *w.r.t.* π . Hence if:

$$\frac{du^*}{d\pi} > 0 \Rightarrow \frac{\pi}{u^*} \frac{du^*}{d\pi} > 0$$

then:

$$\frac{dg^*}{d\pi}, \frac{dr^*}{d\pi} > 0$$

The economy is now unequivocally profit-led!



Meanwhile, if:

$$\frac{du^*}{d\pi} < 0$$

and:

$$\left|\frac{\pi}{u^*}\frac{du^*}{d\pi}\right| > 1$$

(u^* is π -elastic) then:

$$\frac{dg^*}{d\pi}, \frac{dr^*}{d\pi} < 0$$

The economy is unequivocally *wage-led* again (as in the Kaleckian model). The paradox of costs is restored!

Finally, if:

$$\frac{du^*}{d\pi} < 0$$

but:

$$\left|\frac{\pi}{u^*}\frac{du^*}{d\pi}\right|<1$$

(u^* is π -inelastic) then:

$$\frac{dg^*}{d\pi}, \frac{dr^*}{d\pi} > 0$$

The economy is neither unequivocally wage- nor profit-led.

To summarize (and use Bhaduri-Marglin's terminology):

| $\partial u^*/\partial \pi$ | Signs of partial derivatives | | |
|-----------------------------|------------------------------|------------------------------|-----------------|
| | - | - | + |
| $\partial g^*/\partial \pi$ | _ | + | + |
| $\partial r^*/\partial \pi$ | - | + | + |
| Terminology | Cooperative stagnationist | Conflictual stagnationist | Exhilarationist |

Bhaduri-Marglin: a summing up

- ► Bhaduri-Marglin claim to offer a *generalization* of the distribution-growth relationship
- ▶ BUT don't forget controversy about behavioural basis of model (is $g = g(\pi, u)$ "correct"?)
- Similar results can be obtained by other means:
 - saving out of wages
 - open-economy effects
- But these also controversial:
 - are models with saving out of wages stock-flow consistent?
 - world is a closed economy



A selected menu of new topics

Various extensions and new developments merit exploration, including (but not limited to):

- Autonomous-demand-led growth
- Shifting equilibrium, pseudo instability, and cyclical growth
- Monetary and financial determinants of growth
- Debt-financed consumption spending and the accumulation of household debt
- Wage inequality
- Technical change and the supply side



Autonomous-demand-led growth

- ► Motivation: revival of supermultiplier analysis by Sraffians (Freitas and Serrano, 2015)
- ▶ In Sraffian supermultiplier model, level of output (but not g) is wage-led
- ➤ This has given rise to new Kaleckian interpretation of wage-led growth in presence of autonomous demand (Allain, 2015; Lavoie, 2016)

Autonomous-demand-led growth (cont.)

Key innovation:

$$S = s_{\pi}\Pi - A$$

so that $\Pi=0\Rightarrow S=-A<0$ – i.e., capitalists dis-save to fund autonomous consumption (A)

Autonomous-demand-led growth (cont.)

Now assume I = S and standardize by K:

$$\left. \frac{I}{K} \right|_{I=S} = \frac{s_{\pi}\Pi}{K} - \frac{A}{K}$$

$$\Rightarrow g^s = s_{\pi}r - a$$

where
$$a = \frac{A}{K}$$

Note that:

$$a=\frac{A}{K}$$

$$\Rightarrow \dot{a} = a(\hat{A} - \hat{K})$$

$$\Rightarrow \dot{a} = a(\bar{g}_A - g)$$

We now have a new dynamic, driving a new adjusting variable (a), towards a new steady-state condition $\dot{a}=0 \Leftrightarrow \bar{g}_A=g$



To bring all this into focus, consider the simplified Kaleckian model:

$$g = g(u)$$

$$g^s = s_{\pi}r - a = \frac{s_{\pi}\pi u}{v} - a$$

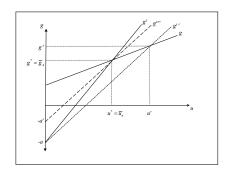
and now suppose that the profit share of income, π , falls

Result:

$$\blacktriangleright$$
 $\downarrow \pi \Rightarrow \uparrow u, g \dots$

$$ightharpoonup ... g > \bar{g}_A \Rightarrow \dot{a} < 0 ...$$

• ... until
$$a = a'$$
, where $g = g^* = \bar{g}_A$ (and $u = u^* = \bar{u}_n$)



Interpretation:

- $ightharpoonup \Delta\pi$ has no effect on *steady-state* outcomes ...
- ... so no influence of distribution on growth specifically, no paradox of costs?
- Alternatively:
 - ightharpoonup since $\downarrow \pi \Rightarrow g > \bar{g}_A$ during traverse ...
 - ightharpoonup ... so that average value of g exceeds \bar{g}_A in 'long run' ...
 - ... growth remains wage-led: paradox of costs survives
- Note connection to 'history versus equilibrium' theme (focus on traverse). Which brings us to ...



Shifting equilibrium, pseudo instability, and cyclical growth

- ► Motivation: 'history versus equilibrium' theme
- Key innovation: state of long-term expectations ('animal spirits') influenced by short-term expectational disappointment (Kregel, 1976)
 - since animal spirits influence parameters of investment function ...
 - ... and thus the value of the equilibrium rate of growth ...
 - ... disequilibrium will now affect the position of equilibrium giving rise to 'shifting equilibrium' analysis

Consider the following simplified Kaleckian model:

$$g = \gamma_1 + \gamma_2 u^e$$

$$g^s = s_\pi \pi u$$

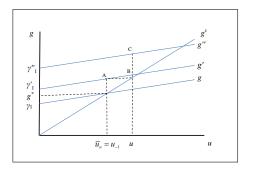
$$u^{e} = u_{-1}$$

$$\dot{\gamma}_1 = \alpha(u - u^e) = \alpha(u - u_{-1})$$
 , $\alpha > 0$



Starting at at g^* , \bar{u}_n , assume initial $\uparrow \gamma_1$ to γ_1' :

- ▶ $g > g^s$ at A $\Rightarrow \uparrow u \Rightarrow$ movement to B: Keynesian stability condition holds
- ▶ BUT $u > u_1 \Rightarrow \dot{\gamma}_1 > 0 \Rightarrow$ movement to C: shifting equilibrium

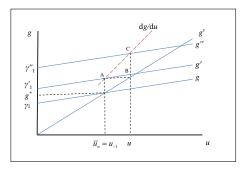


- Economy 'chasing a moving target' may not converge
- Result: 'pseudo-instability'
 - Keynesian stability condition holds ...
 - \blacktriangleright ... but increases (decreases) in g and u self-reinforcing
- Invites addition of turning point mechanisms
- ► E.g., 'second differences matter': $\Delta u > 0$ but
- $\Delta u \Delta u_{-1} = \Delta^2 u < 0 \Rightarrow \downarrow \gamma_1$ and vice versa
- Result cyclical growth



Note also that following initial $\uparrow \gamma_1$:

- Cyclical growth may occur around (never realized) value of $u = \bar{u}_n$
- ► Keynesian stability condition holds, but movement from A to C means $\frac{dg}{du} > \frac{dg^s}{du}$
- Harrodian criticisms addressed!



- Motivation(s): 'financialization'; PK growth real-side only –
 'Hamlet without the Prince' (Kregel, 1985)
- ▶ Post-1980, much more attention to monetary and financial influences on distribution and growth
- Developments nicely summarized in Hein (2014, chpts.9 & 10)

Key innovation: introduction of third claimant (rentiers) on total income

$$Y \equiv wN + \Pi$$

$$\Pi = \Pi_F + iD$$

$$\Rightarrow Y = wN + \Pi_F + iD$$

Hence:

$$S = s_W wN + s_\pi \Pi_F + s_R iD$$



Now assume
$$s_W = 0, s_\pi = 1, 0 < s_R < 1$$
. Then:

$$S = \Pi_F + s_R iD$$

$$\Rightarrow S = \Pi - iD + s_R iD$$

$$\Rightarrow S = \Pi - (1 - s_R)iD$$

Now assume I = S and standardize by K:

$$\frac{I}{K}\Big|_{I=S} = \frac{\Pi}{K} - (1 - s_R)i\frac{D}{K}$$
$$\Rightarrow g^s = \frac{\pi u}{K} - (1 - s_R)i\lambda$$

where
$$\lambda = \frac{D}{K}$$

Note:

- - debt dynamics now part of the picture
 - $\lambda = 0 \Leftrightarrow \hat{D} = g$ required for steady state
 - steady-state debt:income ratio sustainable?
- With $g^s = \frac{\pi u}{v} (1 s_R)i\lambda$:
 - $ightharpoonup \uparrow i, \lambda \Rightarrow \downarrow g^s \dots$
 - ... so *ceteris paribus*, rentier claims boost *C* ...
 - ... but other things aren't equal ...



Now have:

$$g=\gamma+g_{u}u+g_{r}r_{F}$$
 where $r_{F}=rac{\Pi-iD}{K}=r-i\lambda$ $\Rightarrow g=\gamma+g_{u}u+g_{r}(r-i\lambda)$

$$\Rightarrow g = (\gamma - g_r i \lambda) + g_u u + g_r r$$

So $\uparrow i, \lambda \Rightarrow \downarrow g$: ceteris paribus, rentier claims reduce I



So, if rentier claims on income rise, does economy improve or deteriorate? Depends:

- ▶ If firms 'hoard' retained earnings $(g_r \text{ low})$ and rentiers free-spending $(s_R \text{ low})$, g and u increase (dominance of C channel)
- If firms invest retained earnings $(g_r \text{ high})$ and rentiers hoard $(s_R \text{ high})$, g and u decline (dominance of I channel)

Finally, note that we can replace iD with ρE , where:

- ► E denotes shareholders' equity
- \triangleright ρ denotes dividend rate earned by shareholders

Provides basis for interpreting rentier claims in terms of 'shareholder value' movement (extraction of profit from firms at expense of their capital development)

- Motivated by coincident rise of inequality and household borrowing
- Large literature on this theme
- ▶ PK models linking inequality and household borrowing to distribution and growth include (*inter alia*) Kapeller and Schütz (2015); Setterfield and Kim (2017, 2020)

Key innovation(s):

$$C = C_W + C_R + \dot{D}$$

where:

$$\dot{D} = \beta (C^T - C_W)$$
 , $\beta > 0$

and:

$$C^T = \eta C_R$$

i.e., 'keeping up with the Joneses'. (Note: this can be augmented with 'running to stand still' effect)



ALSO - how do households service debt? Like a tax:

$$C_W = c_W(WN - iD_R)$$

Or like an expense:

$$C_W = c_W WN$$

and:

$$S_W = (1 - c_W)WN - iD_R$$



Central results:

- 'Consumption-driven, profit-led growth', or paradox of inequality:
 - redistribution towards profit boosts growth ...
 - but not for Bhaduri-Marglin reasons (primacy of I channel)
 - ▶ instead, inequality boosts C because of effects on household borrowing
 - financial sustainability?

- ► Manner in which households service debts matters. When treated as expense:
 - paradox of inequality 'super charged': even transfer of income due to debt servicing boosts C
 - debt dynamics inverted: quadratic debt dynamics yield two steady-state debt:income ratios, with the *larger* of these now the *stable* solution – further challenge to financial sustainability

Wage inequality

- Motivation: much of the observed increase in inequality due to increased wage inequality
- Key innovation distinction between:
 - production workers actually engage in production process
 - supervisory workers (managers) oversee production process

Wage inequality (cont.)

In PK models of distribution and growth, this innovation incorporated in different ways:

- Two-class models, with capitalist-managers who claim part of total wage income
- Three-class models
 - capitalists, supervisory workers, production workers
 - wage bill divided between supervisory workers and production workers

Wage inequality (cont.)

Example: Palley (2017) two-class model

Assume ϕ_W is production workers' share of WN and (because $s_W \neq 0$ and a la Pasinetti (1962)) δ_W their share of Π . Then:

$$S = S_W + S_K = s_W(\phi_W WN + \delta_W \Pi) + s_K([1 - \phi_W]WN + [1 - \delta_W]\Pi)$$

$$\Rightarrow \frac{S}{K} \frac{K}{K_u} \frac{K_u}{Y} = s_W(\phi_W[1-\pi] + \delta_W \pi) + s_K([1-\phi_W][1-\pi] + [1-\delta_W]\pi)$$

$$\Rightarrow \frac{S}{K} \frac{v}{u} = s_W(\phi_W[1-\pi] + \delta_W \pi) + s_K([1-\phi_W][1-\pi] + [1-\delta_W]\pi)$$

Wage inequality (cont.)

Now assume I = S. Then:

$$\frac{I}{K}\bigg|_{I=S} = g^{s} = [s_{W}(\phi_{W}[1-\pi] + \delta_{W}\pi) + s_{K}([1-\phi_{W}][1-\pi] + [1-\delta_{W}]\pi)]\frac{u}{v}$$

Key result: $\uparrow \phi_W, \delta_W \Rightarrow \downarrow g^s$ if $s_W < s_K$

- Economy can still be profit-led
- ▶ BUT redistribution of wage *or* profit income towards production workers with $\pi = \bar{\pi}$ expansionary (via *C* channel)
- New twist on 'wage-led growth' theme (worker-led growth!)



Technical change and the supply side

- Motivation: PK models only study impact of distribution on growth via the demand side
- Key innovation impact of distribution on growth via the supply side. Possible because:
 - **Potential** (Harrodian natural) rate of growth, y_p , affected by labour productivity growth
 - labour productivity growth affected by distribution if technical change is induced (by profit squeeze) and factor biased (labour-saving)
- May give rise to growth that is profit-led in medium run, but wage-led in long-run steady state, where $g=y_p$ (Rada et al., 2021)

Suppose that:

$$g = g(\pi, \mathbf{Z})$$
 , $g_{\pi} > 0$

$$\pi=1-\omega=1$$
 — wa

where ω is the wage share of income

Then $\uparrow w \Rightarrow \uparrow \omega \Rightarrow \downarrow \pi \Rightarrow \downarrow g$: growth profit-led (a la Bhaduri-Marglin)

Now write:

$$y_p = -\hat{a} + \bar{n} = q + \bar{n}$$

$$q = \gamma \omega$$
 , $\gamma > 0$

$$\hat{w} = q + \delta(g - y_p)$$

Note that in the steady state:

$$g = y_p$$

(constant rate of employment)

$$\Rightarrow \hat{w} = q = -\hat{a}$$

which renders constant the distribution of income ($\omega=wa$, $\pi=1-wa$)

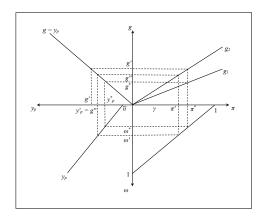
BUT – now assume $\Delta \mathbf{Z} \Rightarrow \uparrow g \Rightarrow g > y_p$ initially:



First,
$$\Delta \mathbf{Z} \Rightarrow \uparrow g \Rightarrow g' > y_p^*$$

Then, $g' > y_p^* \Rightarrow \hat{w} > q \Rightarrow \uparrow \omega$ has two effects:

- $\downarrow \pi \Rightarrow \downarrow g \text{ (profit-led growth effect)}$
- ↑ $q \Rightarrow \uparrow y_p$ (induced, factor-biased technical change effect)



- ▶ RESULT steady-state equilibrium restored when $g = y_p$, consistent with lower g (i.e., g < g') and higher y_p (i.e., $y_p > y_p^*$)
- ► In other words,
 - ▶ although growth profit-led in medium run ...
 - ... steady-state rate of growth increases in response to ↑ w − wage-led!
- ▶ Note consistency with Blecker (2016): growth more likely to be wage-led in long run

Summary and conclusions

- Even confining our attention to functional distribution of income, distribution-growth relationship complicated in PK models:
 - distribution can be endogenous (adjusting) variable (neo-Keynesian) ...
 - ... or exogenous cause of wage- or profit-led outcomes (Kaleckian, Bhaduri-Marglin) ...
 - ... or neither (e.g., steady-state supermultiplier models)
- Relationship between distribution and growth further complicated by extensions to basic (canonical) models

Summary and conclusions (cont.)

- ▶ In addition, distribution-growth relationship draws out controversy concerning treatment of *u* in macrodynamics
 - $u = \bar{u}_n = 1$ versus variable u
 - ▶ variable *u* a *necessary* condition for paradox of costs
 - but not a *sufficient* condition (Bhaduri-Marglin)
- All told, not surprising that distribution and growth remains a lively topic in PK analysis!

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